

Honors PreCalc – Chapter 5 Homework Packet

Simplify each expression

1) $\sin \theta \cdot \csc \theta$

2) $\cot \theta \cdot \sec \theta$

3) $\csc^2 \theta \cdot \cos^2 \theta$

4) $\cos^2 \theta \cdot \tan \theta \cdot \sec \theta$

5) $\sin \theta (\csc \theta - \sec \theta)$

6) $\frac{\sec^2 \theta}{\tan^2 \theta}$

7) $\sec \theta (\sec^2 \theta - 1) + \sec \theta$

8) $\frac{\csc^2 \theta \cdot \cos^2 \theta}{\tan^2 \theta}$

9) $\tan \theta (\cos \theta + 2 \cot \theta)$

10) $\csc^2 \theta (\sin^2 \theta + 1)$

11) $1 - \frac{\sin^2 \theta}{\tan^2 \theta}$

12) $\frac{\sin \theta \cos \theta}{1 - \cos^2 \theta}$

13) $\frac{\tan \theta + \sin \theta \sec \theta}{\csc \theta \tan \theta}$

14) $\frac{\cos \theta}{\sec \theta + 1} + \frac{\cos \theta}{\sec \theta - 1}$

15) $\frac{1 - \sin^2 \theta}{1 - \cos^2 \theta} \cdot \tan \theta$

16) $\frac{\sin^2 \theta + 3 \sin \theta + 2}{\sin^2 \theta + 2 \sin \theta}$

17) $\frac{\cos^2 \theta - \sin^2 \theta}{\cos^2 \theta + \cos \theta \sin \theta}$

Use a two-column proof to prove that one side of the equation is equal to the other side. Give reasons for each step.

$$18) \sin^2 \theta \sec \theta \csc \theta = \tan \theta$$

$$19) \csc \theta - \sin \theta = \cot \theta \cos \theta$$

$$20) \tan \theta [\cos(90^\circ - \theta) + \cot \theta \cos \theta] = \sec \theta$$

$$21) \frac{1}{\sin \theta \cos \theta} - \frac{\cos \theta}{\sin \theta} = \tan \theta$$

Transform one side of the equation to the other side.

$$22) \frac{1 + \cot^2 x}{\sec^2 x} = \cot^2 x$$

$$23) \frac{\sec \theta}{\sin \theta} - \frac{\sin \theta}{\cos \theta} = \cot \theta$$

$$24) \frac{1}{\sec x - \tan x} + \frac{1}{\sec x + \tan x} = 2 \sec x$$

$$25) \frac{\cos \theta}{\sec \theta - 1} - \frac{\cos \theta}{\tan^2 \theta} = \cot^2 \theta$$

$$26) \sec^2 x + \csc^2 x = \sec^2 x \csc^2 x$$

$$27) \frac{1 - 3 \cos \theta - 4 \cos^2 \theta}{\sin^2 \theta} = \frac{1 - 4 \cos \theta}{1 - \cos \theta}$$

$$28) \frac{\sin \theta}{1 + \cos \theta} + \frac{1 + \cos \theta}{\sin \theta} = 2 \csc \theta$$

$$29) \frac{1}{\sec x - \tan x} = \sec x + \tan x$$

$$30) \frac{1}{\sec^2 x} + \frac{1}{\csc^2 x} = 1$$

$$31) \frac{\sin^3 x + \cos^3 x}{\sin x + \cos x} = 1 - \sin x \cos x$$

32) Write out each of the six trig functions in terms of $\sin \theta$.

33) Fill in each blank with an angle measure that would make the statement true.

$$\csc 11^\circ = \sec \underline{\hspace{2cm}}$$

$$\tan 42^\circ = \cot \underline{\hspace{2cm}}$$

$$\sin \frac{\pi}{7} = \cos \underline{\hspace{2cm}}$$

$$\cos 147^\circ = \sin \underline{\hspace{2cm}}$$

$$\tan \frac{52\pi}{17} = \cot \underline{\hspace{2cm}}$$

$$\sec 312^\circ = \csc \underline{\hspace{2cm}}$$

Simplify.

34) $\sin 75^\circ \cos 15^\circ + \cos 75^\circ \sin 15^\circ$

35) $\cos \frac{5\pi}{12} \cos \frac{\pi}{12} - \sin \frac{5\pi}{12} \sin \frac{\pi}{12}$

36) $\sin 3x \cos 2x - \cos 3x \sin 2x$

37) $\cos 2x \cos x + \sin 2x \sin x$

38) $\frac{\tan 100^\circ + \tan 50^\circ}{1 - \tan 100^\circ \tan 50^\circ}$

39) $\frac{\tan \frac{2\pi}{3} + \tan \frac{\pi}{12}}{1 - \tan \frac{2\pi}{3} \tan \frac{\pi}{12}}$

$$40) \frac{\tan 2\theta - \tan \theta}{1 + \tan 2\theta \tan \theta}$$

$$41) \cos \frac{\pi}{2} \cos x + \sin \frac{\pi}{2} \sin x$$

$$42) \sin 3y \cos y + \cos 3y \sin y$$

$$43) \cos\left(\frac{\pi}{3} + \theta\right) + \cos\left(\frac{\pi}{3} - \theta\right)$$

$$44) \frac{\sin(\alpha + \beta) + \sin(\alpha - \beta)}{\cos \alpha \cos \beta}$$

$$45) \frac{\cos(\alpha + \beta) + \cos(\alpha - \beta)}{\sin \alpha \sin \beta}$$

Determine the exact value.

$$46) \sin \frac{11\pi}{12}$$

$$47) \cos 15^\circ$$

$$48) \sec \frac{5\pi}{12}$$

$$49) \tan 105^\circ$$

50) Suppose that $\sin \alpha = \frac{4}{5}$ and $\sin \beta = \frac{1}{2}$ where $\frac{\pi}{2} < \beta < \alpha < \pi$. Evaluate $\sin(\alpha - \beta)$.

51) Suppose that $\tan \alpha = \frac{4}{3}$ and $\tan \beta = \frac{12}{5}$ where $0 < \alpha < \beta < \frac{\pi}{2}$. Evaluate $\cos(\alpha - \beta)$.

52) Given that $\sin \alpha = \frac{12}{13}$ and $\cos \beta = -\frac{4}{5}$, where $0 < \alpha < \frac{\pi}{2} < \beta < \pi$, evaluate $\sin(\beta - \alpha)$.

53) Given that $\tan \alpha = 2$ and $\tan \beta = -\frac{1}{3}$, determine $\tan(\alpha + \beta)$ and $\tan(\alpha - \beta)$

54) Prove: $\cos\left(\frac{\pi}{2} + x\right) = -\sin x$

55) Suppose $\sin A = \frac{5}{13}$ and $\frac{\pi}{2} < A < \pi$. Suppose $\tan B = \frac{7}{24}$ and $\pi < B < \frac{3\pi}{2}$. Determine the following values.

a) $\cos 2B$

b) $\sec(A - B)$

c) $\sin(2A)$

d) $\tan(A + B)$

e) $\tan(2A)$

f) $\sin(A + B)$

56) Use trigonometric identities to simplify each expression. Leave as an exact answer with a positive argument.

a) $2\cos^2 35^\circ - 1$

b) $\sin \frac{\pi}{7} \cos \frac{\pi}{7}$

c) $6\sin x \cos x$

d) $0.5 - \sin^2 b$

e) $\sin 11^\circ \sin 11^\circ - \sin 79^\circ \cos 11^\circ$

f) $\frac{\tan \frac{\pi}{3} - \tan(-\frac{\pi}{5})}{1 - \tan \frac{\pi}{3} \tan \frac{\pi}{5}}$

g) $\frac{1 - \cos 80^\circ}{2}$

h) $\frac{\cos 64^\circ + 1}{2}$

i) $\frac{2 \tan Y}{1 - \tan^2 Y}$

j) $2\sin u \cos u$

k) $1 - 2\sin^2(p)$

57) Prove: $\sin\left(x + \frac{\pi}{3}\right) + \sin\left(x - \frac{\pi}{3}\right) = \sin x$

58) Prove: $\csc 2A = \frac{\csc A}{2 \cos A}$

59) Write $\cos^4 x$ as the sum or difference of cosines that are raised to the first power.

60) Write the expression $\cos(2 \arcsin x)$ as an algebraic expression.

61) Suppose $\tan A = \frac{3}{4}$ and $180^\circ < A < 270^\circ$. What is $\sin\left(\frac{1}{2}A\right)$, $\cos\left(\frac{1}{2}A\right)$, and $\tan\left(\frac{1}{2}A\right)$?

62) Solve the equation for $0 \leq \theta < 2\pi$.

a) $\sin \frac{\theta}{2} = -1$

b) $\cos \theta - 1 = \sin^2 \theta$

c) $\sin 2\theta \cos \theta = \sin \theta$

d) $\cos 2\theta = -2\cos^2 \theta$

e) $\tan 2\theta - \tan \theta = 0$

f) $\cos(2\theta + \pi) = -1$

g) $\sin 3\theta = \cos 3\theta$

h) $-6 + 10\cos\left(\theta + \frac{\pi}{2}\right) = -1$

63) Solve for $x \in \mathbb{R}$: $\sin(2x) = -\frac{4}{5}$

64) Solve for $x \in \mathbb{R}$: $7\sin^2 x - 1 = 4$

65) Solve for $x \in \mathbb{R}$: $15 = 1 - 7\cot(x + 6^\circ)$

66) Solve for $\theta \in [0, 2\pi)$: $4\sin^2 \theta + 8\sin \theta = -3$

Solve the following questions for $x \in [0, 2\pi)$.

67) $1 + \cos x = -\sin x$

68) $\frac{\sin\left(\frac{\pi}{2} - x\right)}{\sin x} = -\sqrt{3}$

69) $\cos x - \sqrt{3} \sin x = 1$

70) $\csc x + \cot x = 1$

71) $\sin\left(x + \frac{\pi}{2}\right) - \cos^2 x = 0$

72) $\tan^2 x + 4 \tan x = 6$

Solve the following equations for $x \in \mathbb{R}$ (in degrees).

73) $\sec^2(5x) - 1 = 16$

74) $2 \cos^2\left(\frac{1}{2}x\right) - 2 = 2 \cos x$

75) $\sin 3x \cos 80^\circ - \sin 80^\circ \cos 3x = -0.36$

76) Determine the general solution(s) of the equation in radians.

a) $2 \sin^2 \theta \tan \theta = \tan \theta$

b) $\tan^2 3\theta = 3$

c) $\sin 3\theta = -\frac{\sqrt{3}}{2}$

d) $\cos \theta \csc^2 \theta + 3 \cos \theta = 7 \cos \theta$